(b) Distinguish between eurelian path and circuit with suitable example.
9. (a) Draw all spanning trees of graph given below : 10

(b) Distinguish between Hamilton path and circuit by taking suitable example.

## 24041

## B. Tech. 3rd Semester (CS \& IT)

Examination - December, 2018

## DISCRETE STRUCTURE

Paper: CSE-203-F
Time : Three Hours ]
[ Maximum Marks : 100
Before answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard, will be entertained after examination.

Note: Attempt five questions in total selecting one question from each of four Sections: Question No. 1 is compulsory.

1. Explain the following terms by taking suitable example :
(i) Equivalence relations and partitioning
(ii) Polynomials and their evaluation
(iii) Integral Domain and fields
(iv) Multi graph and Weighted graph

## SECTION - A

2. Define propositions, tautologies, contradictions and hence prove that the following propositions are tautology :
(i) $\mathrm{pv} \sim \mathrm{p}$
(ii) $\sim(p \wedge q) \vee q$
(iii) $P=>(p \vee q)$
3. (a) Let $\mathrm{f}: \mathrm{A} \rightarrow \mathrm{B}$ be a function. Then show that $\mathrm{f}-1$ exists iff $f$ is a bijective function.
(b) Consider the following conditional statement:
p : if the flood destroy my house or the fire destroy my house, then my insurance company will pay me.
(c) Let $\mathrm{A}=\{1,2,3,4\}$ and $\mathrm{R}=\{(2,1),(3,1),(3,2),(4,1),(4,2)$, $(4,3),(1,1),(2,2)\}$ Show that $R$ is Equivalence Relation or not.

## SECTION - B

4. (a) Explain permutations and combination and hence find in how many ways a committee of 3 faculty members and four students be selected from 6 faculty members and 6 students.
(b) Define AP, GP and AG series with examples. Also write the formula for sum of $n$ terms in AP, GP, AG series.
5. (a) Solve the recurrence relation:
$a_{r}-7 a_{r-1}+10 a_{r-2}+20=0$ by the method of generating functions with the initial conditions $a_{0}=3$ and $a_{1}=3$.
(b) Solve the recurrence relations:
$a_{r}-4 a_{r-1}+4 a_{r-2}=0$ and find the particular solution, given that $a_{0}=3$ and $a_{1}=3$.

## SECTION - C

6. Define the following with suitable example:
(i) Semi group
(ii) Homomorphism
(iii) Cosets
(iv) Integral domain and fields
7. (a) State and prove Lagrange's Theorem. 10
(b) Define with suitable example :
(i) Isomorphism and automorphism
(ii) Normal subgroup

## SECTION - D

8. (a) Find the shortest path from $A$ to $Z$.

