Roll No.

91526

B. Sc. (Hons.) Physics 2nd Sem. Latest Examination – April, 2018

MATHEMATICAL PHYSICS-II

Paper: Phy-201

Time: Three Hours]

[Maximum Marks: 40

Before answering the questions, candidates should ensure that they have been supplied the correct and complete question paper. No complaint in this regard, will be entertained after examination.

Note: Attempt five questions in all selecting at least two questions from each Unit. All questions carry equal marks.

UNIT -

1. State rules for finding the complementary function of a nth order differential equation of the type $(D^n + k_1 D^{n-1} + ... + k_n)y = 0$ in different cases. If y_1 and y_2 are two solutions of this equation, prove that $c_1y_1 + c_2y_2$ is also its solution.

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- **2.** Find complete solution of the following differential equation, $(1-x^2)d^2y/dx^2 2x dy/dx + n(n+1)y = 0;n$ is a constant and discuss the results.
- 3. Describe solution of Cauchy's homogenous equation. Solve $x^2d^2y/dx^2 + x(dy/dx) + y = \log x \sin(\log x)$. 8
- **4.** (i) Determine the singular points at infinity of $x^2d^2y/dx^2 2x(dy/dx) + p^2y = 0$ where p is an integer.
- (ii) Find complete solution of the equation $(D-2)^2 = 8(e^{2x} + \sin 2x + x^2).$

JNIT - II

(i) Represent the following function in Fourier series.

$$F(x) = \begin{cases} -\sin x, & -\pi \le x < 0 \\ \sin x, & 0 < x \le \pi \end{cases}$$

(ii) Show that:

$$\sum_{n=1}^{\infty} (-1)^{n+1} \frac{\sin nx}{n} = \frac{x}{2}$$

- **6.** (i) Represent the function $x \sin x$ in Fourier series. 4
- (ii) Find the value of Σ1/n² using Fourier series for the function f(x) = x².
- 91526-500 -(P-3)(Q-8)(18) (2)

- right circular cylinder of radius 1.5 m and length 4m and is surmounted by hemispherical ends. If the radius increased by 0.01 m and length by 0.05 m, find the percentage change in volume of the balloon.
- Explain Fourier sine and cosine series. Obtain the Fourier series representation for a full wave rectifier.