M. Tech 1st Semester (Civil Enggineering Computer Aided Structural Engg.) Examination, December-2023 THEORY OF ELASTICITY

Paper-21MTCASE21C3

Time allowed: 3 hours]

[Maximum marks : 100

Note: Question 1 is compulsory. Attempt one question from each Section. All questions carry equal marks.

Assume missing data, if any, suitably.

- 1. (a) What is elasticity?
 - (b) Write Saint Venant's principle.
 - (c) Write applications of polar coordinates and advantages of considering problem using polar coordinates.
 - (d) What do you mean by traction boundary conditions?
 - (e) What is contraction applied to tensors?
 - (f) Classify isotropic tensors
 - (g) What is the difference between strain energy and complementary energy.
 - (h) Write principle of linear superposition.

 $2.5 \times 8 = 20$

Section-A

- 2. Explain the procedure for determination of stresses on any plane inclined to regular set of axes. The inclination of the plane is defined by direction cosines.
- 3. Discuss Hooks law.

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Section-B

4. The components of a first-and second-order tensor in a particular coordinate frame are given. Determine the components of each tensor in a new coordinate system found through a rotation of 60° ($\pi/3$ radians) about the x3-axis.

$$\mathbf{a}_{i} = \begin{bmatrix} 1 \\ 4 \\ 2 \end{bmatrix}, \ \mathbf{a}_{ij} = \begin{bmatrix} 1 & 0 & 3 \\ 0 & 2 & 2 \\ 3 & 2 & 4 \end{bmatrix}$$

5. Explicitly verify the following properties of the Kronecker delta 20

$$\delta_{ij}a_j=a_i$$

$$\delta_{ij}a_{jk} = a_{ik}$$

Section-C

6. Investigate what problem of plane stress is solved by the stress function 20

$$\phi = \frac{3F}{4c}(xy - \frac{xy^3}{3c^2}) + \frac{P}{2}y^2$$

7. Show that-

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$$\phi = \frac{q}{8c^3} \left[x^2 (y^3 - 3c^2y + 2c^3) - \frac{1}{5} y^3 (y^2 - 2c^2) \right]$$

Is a stress function and find what problem it solves when applied to the region included in $y = \pm c$, x = 0, on the side x positive.

Section-D

- 8. Find an expression in terms of α_x , α_y , ι_{xy} for strain energy V per unit thickness of a cylinder or prism in plane strain $(\in x = 0)$.
- Explain in detail-

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- (a) Principle of linear superposition
- (b) Clapeyron's theorem